STAT 561: Logistic Regression

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# 1. Absenteesim data

absent <- read\_excel("Absenteeism\_at\_work.xls")

## Recode and Factor Conversion

absent <- absent %>%  
 mutate(absenteeism = case\_when(  
 Absenteeism\_time\_in\_hours >= 0 & Absenteeism\_time\_in\_hours <= 20 ~ "Low",  
 Absenteeism\_time\_in\_hours > 20 & Absenteeism\_time\_in\_hours <= 40 ~ "Moderate",  
 Absenteeism\_time\_in\_hours > 40 ~ "High"  
 ))  
  
absent$absenteeism <- factor(absent$absenteeism, levels = c("Low", "Moderate", "High"))  
absent$Day\_of\_the\_week <- factor(absent$Day\_of\_the\_week,  
 levels = 2:6,  
 labels = c("Monday", "Tuesday", "Wednesday", "Thursday", "Friday"))  
absent$Seasons <- factor(absent$Seasons,  
 levels = 1:4,  
 labels = c("Summer", "Autumn", "Winter", "Spring"))  
absent$Education <- factor(absent$Education,  
 levels = 1:4,  
 labels = c("High School", "Graduate", "Postgraduate", "Master/Doctor"))

## (a) How is the ‘Absenteeism time in hours’ distributed? Are there any noticeable patterns or outliers?

**Interpretation:**

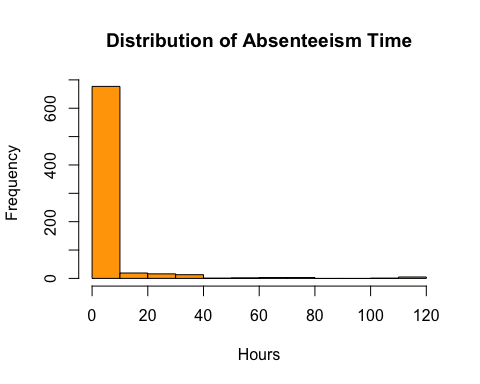
**In Histogram:** The histogram of Absenteeism\_time\_in\_hours reveals a highly right-skewed distribution. Most of the values are clustered at the lower end of the scale. These values suggest that short-term absences (below 10 hours) are extremely common, likely reflecting partial or single-day absences.

**In box-plot:** Yes, there are 10 outliers in the data. A noticeable pattern is that long-term absences are very rare, while short-term absences are very common.

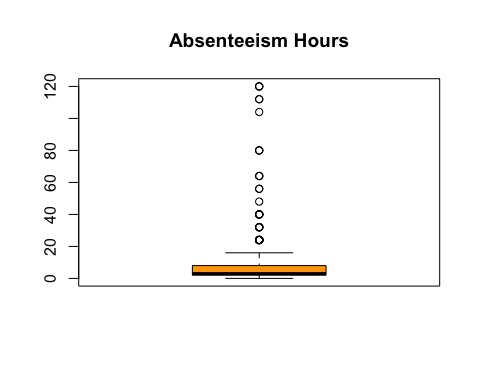
table(absent$Absenteeism\_time\_in\_hours)

##   
## 0 1 2 3 4 5 7 8 16 24 32 40 48 56 64 80 104 112 120   
## 44 88 157 112 60 7 1 208 19 16 6 7 1 2 3 3 1 2 3

hist(absent$Absenteeism\_time\_in\_hours, main = "Distribution of Absenteeism Time",  
 xlab = "Hours", col = "orange")



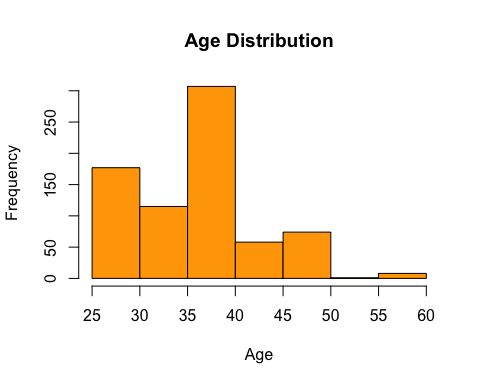
#summary(absent['Absenteeism\_time\_in\_hours'])  
boxplot(absent$Absenteeism\_time\_in\_hours, main = "Absenteeism Hours", col = "orange")



## (b) What is the distribution of ages among the employees? Are certain age groups more prevalent?

**Interpretation:** The age distribution among employees is right-skewed. Most employees fall within the 35–40 age group, which is the most prevalent. There are also notable numbers in the 25–30 and 30-35 age ranges. Very few employees are older than 50.

hist(absent$Age, main = "Age Distribution", xlab = "Age", col = "orange")



## (c) Is there a correlation between the distance from residence to work and absenteeism time?

**Interpretation:** The correlation coefficient between distance from residence to work and absenteeism time in hours is -0.088 which is very close to 0. This indicates that there is very weak negative correlation between these two. We can also see from the plot that the regression line is almost horizontal. So in practical terms, it suggest that distance to work does not significantly influence how much time employees are absent.

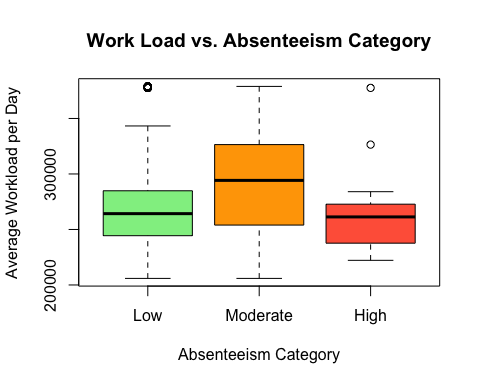
cor(absent$Distance\_from\_Residence\_to\_Work, absent$Absenteeism\_time\_in\_hours, use = "complete.obs")

## [1] -0.08836282

## (d) How does the work load average per day relate to absenteeism? Are higher workloads associated with more or less absenteeism?

**Interpretation:** The boxplot shows that moderate absenteeism is associated with the highest average workload per day, while low absenteeism corresponds to the lowest average workload. This suggests that higher workloads are not associated with more absenteeism—in fact, employees with higher absenteeism tend to have lower workloads.

boxplot(Work\_load\_Average\_in\_days ~ absenteeism, data = absent,  
 main = "Work Load vs. Absenteeism Category",  
 xlab = "Absenteeism Category", ylab = "Average Workload per Day",  
 col = c("lightgreen", "orange", "tomato"))



aggregate(Work\_load\_Average\_in\_days ~ absenteeism, data = absent, FUN = mean)

## absenteeism Work\_load\_Average\_in\_days  
## 1 Low 270579.9  
## 2 Moderate 296701.5  
## 3 High 264988.1

## (e) Analyze the absenteeism based on education levels. Do certain education levels correlate with higher or lower absenteeism?

**Interpretation:** The analysis of absenteeism based on education level reveals the following patterns:

**a.**Low absenteeism is most common among individuals with a high school education. This group has the highest frequency overall, suggesting that employees with lower educational attainment tend to have fewer absences.

**b.**In the moderate absenteeism category, the graduate level shows the highest frequency, though the overall numbers in this category are relatively low compared to the low absenteeism group.

**c.**For high absenteeism, the postgraduate group has the highest frequency, indicating that individuals with higher education levels might be more prone to higher absenteeism, although the total count is still small.

**Conclusion:**

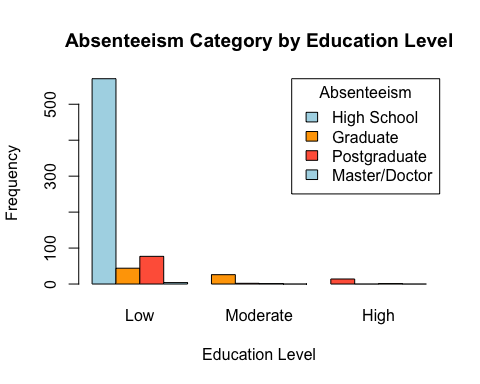
* High school–educated individuals are more frequently associated with low absenteeism.
* Postgraduates appear slightly more often in the high absenteeism group.

However, the statistical test (Chi-square) yielded a non-significant result (p = 0.7608), indicating that there is no strong statistical evidence of a correlation between education level and absenteeism in this dataset.

# For a single categorical column  
table(absent$Education)

##   
## High School Graduate Postgraduate Master/Doctor   
## 611 46 79 4

edu\_abs\_table <- table(absent$Education, absent$absenteeism)  
  
barplot(edu\_abs\_table,   
 beside = TRUE,   
 col = c("lightblue", "orange", "tomato"),  
 legend.text = TRUE,  
 args.legend = list(title = "Absenteeism", x = "topright"),  
 main = "Absenteeism Category by Education Level",  
 xlab = "Education Level",  
 ylab = "Frequency")



chisq.test(edu\_abs\_table)

## Warning in chisq.test(edu\_abs\_table): Chi-squared approximation may be  
## incorrect

##   
## Pearson's Chi-squared test  
##   
## data: edu\_abs\_table  
## X-squared = 3.3725, df = 6, p-value = 0.7608

## (f) Which variables show the strongest correlation with absenteeism time in hours? How might these influence your logistic regression model?

**Interpretation:** From the correlation results, we can see that the variable with the strongest (though still relatively weak) correlation with Absenteeism\_time\_in\_hours is:

Height – correlation: 0.144

Although the correlations are generally low, the variable may still provide predictive value when combined with others in a logistic regression model, especially when capturing nonlinear relationships or interactions. Height surprisingly shows the highest correlation. Might act as a proxy for health or physical condition but needs further domain investigation.

num\_vars <- absent %>% select\_if(is.numeric)  
cor\_matrix <- cor(num\_vars, use = "complete.obs")  
cor\_with\_absence <- cor\_matrix[, "Absenteeism\_time\_in\_hours"]  
cor\_with\_absence\_sorted <- sort(abs(cor\_with\_absence), decreasing = TRUE)  
cor\_with\_absence\_sorted

## Absenteeism\_time\_in\_hours Height   
## 1.00000000 0.14442048   
## Son Distance\_from\_Residence\_to\_Work   
## 0.11375650 0.08836282   
## Age Body\_mass\_index   
## 0.06575970 0.04971948   
## Pet Transportation\_expense   
## 0.02827659 0.02758463   
## Work\_load\_Average\_in\_days Month\_of\_absence   
## 0.02474890 0.02434536   
## Service\_time ID   
## 0.01902926 0.01799659   
## Weight   
## 0.01578918

## (g) Are there any unexpected correlations or findings that challenge common assumptions about workplace absenteeism?

**Interpretation:** Yes, there are some unexpected correlations.

1. Height has the strongest correlation (r = 0.144)

**Challenge to assumption:** Height is not commonly associated with absenteeism in workplace literature. This is unexpected because we typically expect health, stress, or distance to play a stronger role. This could be a spurious correlation, or height might be correlated with another latent variable like overall physical health or job type (e.g., taller individuals in more physically demanding roles).

1. Weak correlation with Distance from Residence to Work (r = 0.088)

**Challenge to assumption:** Many assume that longer commutes lead to higher absenteeism due to fatigue, delays, or dissatisfaction. Here, distance has only a mild correlation, suggesting that commute distance might not be a strong standalone predictor—or that employees have adjusted to their commute.

1. Minimal correlation with Body Mass Index (BMI) and Weight (r ≈ 0.05)

**Challenge to assumption:** Health-related metrics like BMI are often thought to influence absenteeism due to illness. The weak correlation suggests that BMI/weight alone may not be a strong predictor of time missed from work, perhaps due to health-conscious policies or remote work flexibility.

## (h) Does service time (duration of service in the company) have any impact on the absenteeism rate?

**Interpretation:** The correlation between Service Time and Absenteeism Time in Hours is 0.019, which is very close to zero. This means there is very less linear relationship between how long an employee has worked at the company and how much time they are absent. In other words, service time does not appear to influence absenteeism in a meaningful way.

cor(absent$Service\_time, absent$Absenteeism\_time\_in\_hours, use = "complete.obs")

## [1] 0.01902926

## (i) Examine if day of the week has any influence on absenteeism – are certain days more prone to absences?

**Observations:**

Yes, based on the bar chart, here are some observations:

Monday has the highest number of absences, followed closely by Wednesday and Tuesday.

Friday has the lowest number of absences, noticeably lower than other weekdays.

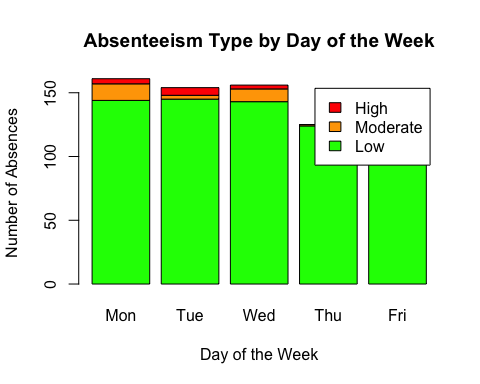
Most absences on all days are classified as low (green).

Moderate (orange) and high (red) absences occur more on Monday and Wednesday, slightly tapering off through the week.

**Interpretation:**

Yes, the day of the week does influence absenteeism.Employees are more likely to be absent on Mondays, possibly indicating extended weekends or recovery from weekends (a common trend in workplace data).The sharp drop in absences on Fridays suggests people might be more likely to show up just before the weekend.

#table(absent$Day\_of\_the\_week)  
day\_abs <- table(absent$Day\_of\_the\_week, absent$absenteeism)  
barplot(t(day\_abs),  
 main = "Absenteeism Type by Day of the Week",  
 col = c("green", "orange", "red"),  
 xlab = "Day of the Week",  
 ylab = "Number of Absences",  
 legend = TRUE,  
 names.arg = c("Mon", "Tue", "Wed", "Thu", "Fri"))



## (j) Identify any outliers in the data set. What could be the reasons for these anomalies, and how might they affect the analysis?

**Observation:**

**Outlier detection:** The data set shows outliers in several numeric variables:

Transportation expense: 3 outliers (rows 145, 146, 217)

Service time: 5 outliers (rows 235, 508, 511, 514, 577)

Age: 8 outliers (rows 256, 435, 522, 621, 623, 641, 728, 730)

Work load (Average/day): 32 outliers (rows 205–236)

Pets: 44 outliers (e.g., rows 7, 23, 26, …)

Height: 109 outliers (e.g., rows 2, 9, 21, …)

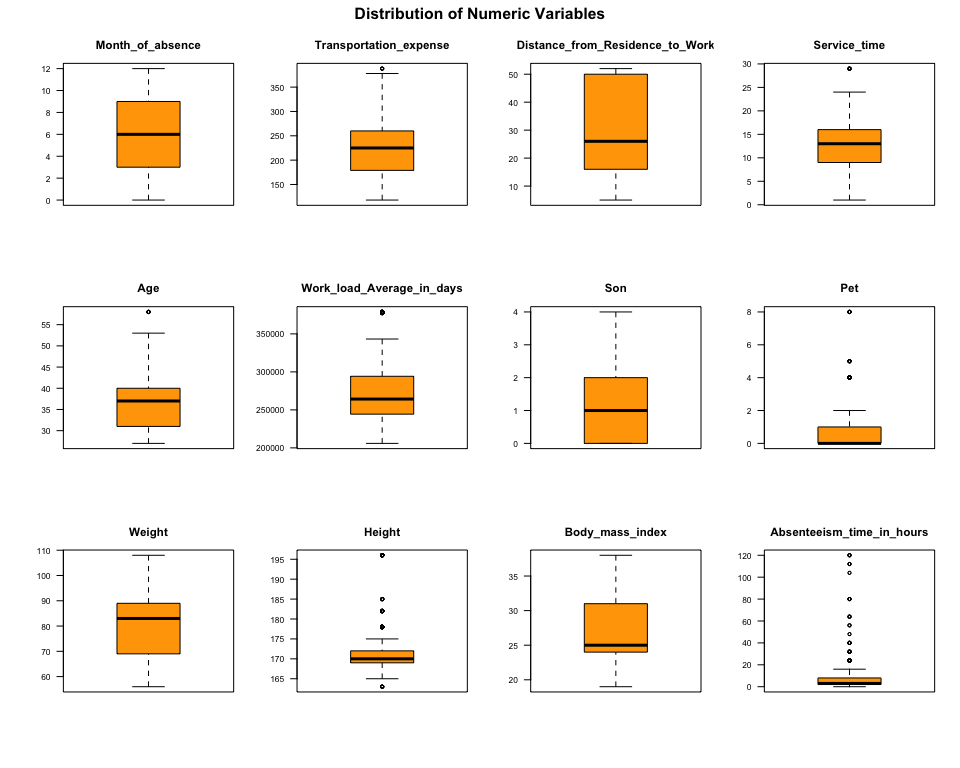
Absenteeism time: 43 outliers (e.g., rows 9, 23, 50, …)

**Potential reasons for outliers and their impact on analysis:**

Outlier Analysis Summary

| Variable | Potential Reasons | Impact on Analysis |
| --- | --- | --- |
| Transportation expense | Company vehicle users; Relocated employees | Inflates average costs |
| Service time | Long-tenured employees; Data entry errors | Distorts tenure relationships |
| Age | Young interns; Employees past retirement | Biases age conclusions |
| Work load (Average/day) | Temporary projects; Tracking errors | Skews workload effects |
| Pets | Animal lovers; Data placeholders | False pet correlations |
| Height | Unit errors; Physiological extremes | Spurious health metrics |
| Absenteeism time | Medical/Parental leave; Sabbaticals | Dominates prediction models |

# Exclude ID column and keep only numeric variables  
numeric\_vars <- absent %>%   
 select(-ID) %>%   
 select\_if(is.numeric)  
  
# Set up 3x4 plotting grid with adjusted margins  
par(mfrow = c(3, 4), mar = c(5, 4, 3, 1), oma = c(1, 1, 2, 1)) # Increased bottom margin  
  
# Create vertical boxplots  
for (var in names(numeric\_vars)) {  
 boxplot(numeric\_vars[[var]],   
 main = var,  
 col = "orange",  
 cex.main = 1.1,   
 cex.axis = 0.8,   
 las = 2,   
 horizontal = FALSE)   
}  
  
# Add overall title  
title("Distribution of Numeric Variables", outer = TRUE, cex.main = 1.5)



par(mfrow = c(1, 1)) # Reset layout  
  
# Outlier detection (unchanged)  
find\_outliers <- function(x) {  
 q1 <- quantile(x, 0.25, na.rm = TRUE)  
 q3 <- quantile(x, 0.75, na.rm = TRUE)  
 iqr <- q3 - q1  
 lower\_bound <- q1 - 1.5 \* iqr  
 upper\_bound <- q3 + 1.5 \* iqr  
 which(x < lower\_bound | x > upper\_bound)  
}  
  
outlier\_list <- lapply(numeric\_vars, find\_outliers)  
outlier\_list

## $Month\_of\_absence  
## integer(0)  
##   
## $Transportation\_expense  
## [1] 145 146 217  
##   
## $Distance\_from\_Residence\_to\_Work  
## integer(0)  
##   
## $Service\_time  
## [1] 235 508 511 514 577  
##   
## $Age  
## [1] 256 435 522 621 623 641 728 730  
##   
## $Work\_load\_Average\_in\_days  
## [1] 205 206 207 208 209 210 211 212 213 214 215 216 217 218 219 220 221 222 223  
## [20] 224 225 226 227 228 229 230 231 232 233 234 235 236  
##   
## $Son  
## integer(0)  
##   
## $Pet  
## [1] 7 23 26 32 34 36 39 79 106 110 201 204 216 220 222 233 247 269 311  
## [20] 323 337 398 400 431 470 475 507 541 555 562 565 595 604 630 657 664 691 702  
## [39] 711 713 715 722 725 727 733 738  
##   
## $Weight  
## integer(0)  
##   
## $Height  
## [1] 2 9 21 28 32 34 39 45 56 65 86 90 101 117 141 145 146 152  
## [19] 153 158 166 168 187 189 193 200 204 206 207 211 215 217 219 227 229 231  
## [37] 232 237 238 241 243 244 245 246 254 262 264 267 285 294 307 310 314 317  
## [55] 324 326 344 356 361 363 367 385 403 404 405 408 415 418 420 421 437 455  
## [73] 459 464 465 470 474 490 499 509 529 535 539 565 570 580 593 595 604 609  
## [91] 610 618 629 649 663 669 671 673 676 677 682 684 686 687 689 693 694 698  
## [109] 699 703 705 712 713 715 716 717 722 725 727  
##   
## $Body\_mass\_index  
## integer(0)  
##   
## $Absenteeism\_time\_in\_hours  
## [1] 9 23 50 86 88 97 100 105 164 165 174 188 192 198 200 213 219 223 232  
## [20] 250 273 280 288 300 324 360 388 421 448 449 472 535 556 570 571 623 649 653  
## [39] 661 683 693 712 730 735

# Multinomial Logistic Regression

## (a) Build a logistic regression model

absent$absenteeism <- relevel(absent$absenteeism, ref = "Low")  
logistic\_model <- multinom(absenteeism ~ . -ID -Absenteeism\_time\_in\_hours, data = absent, trace = FALSE)  
summary(logistic\_model)

## Call:  
## multinom(formula = absenteeism ~ . - ID - Absenteeism\_time\_in\_hours,   
## data = absent, trace = FALSE)  
##   
## Coefficients:  
## (Intercept) Month\_of\_absence Day\_of\_the\_weekTuesday  
## Moderate 51.04294 0.00458543 -1.6548135  
## High 80.05895 0.27859061 0.1237795  
## Day\_of\_the\_weekWednesday Day\_of\_the\_weekThursday Day\_of\_the\_weekFriday  
## Moderate -0.4040314 -2.54564 -2.0695436  
## High -0.5518047 -129.25994 -0.8766896  
## SeasonsAutumn SeasonsWinter SeasonsSpring Transportation\_expense  
## Moderate -0.1056535 0.3905583 0.3779225 0.0066974359  
## High 0.4021068 1.7405336 -0.3553547 -0.0002083499  
## Distance\_from\_Residence\_to\_Work Service\_time Age  
## Moderate 0.01616403 0.07461651 -0.005833977  
## High -0.07024052 -0.18343805 0.088955878  
## Work\_load\_Average\_in\_days EducationGraduate EducationPostgraduate  
## Moderate 8.768406e-06 -0.578137 -1.440652  
## High -6.468366e-06 -128.422933 -1.035359  
## EducationMaster/Doctor Son Pet Weight Height  
## Moderate -66.31024 -0.1038587 -0.6232737 0.4420499 -0.3294649  
## High -101.78414 0.7277251 -0.1921179 0.5805620 -0.4698593  
## Body\_mass\_index  
## Moderate -1.369305  
## High -1.857992  
##   
## Std. Errors:  
## (Intercept) Month\_of\_absence Day\_of\_the\_weekTuesday  
## Moderate 2.530443e-06 3.719697e-05 2.476267e-07  
## High 2.279445e-06 2.302747e-05 1.971105e-06  
## Day\_of\_the\_weekWednesday Day\_of\_the\_weekThursday Day\_of\_the\_weekFriday  
## Moderate 8.192734e-07 1.249114e-07 6.772053e-07  
## High 3.021818e-07 3.381650e-63 2.795676e-06  
## SeasonsAutumn SeasonsWinter SeasonsSpring Transportation\_expense  
## Moderate 6.262522e-07 2.534559e-06 3.049482e-06 0.002380841  
## High 1.224691e-06 2.600527e-06 1.621647e-06 0.003447287  
## Distance\_from\_Residence\_to\_Work Service\_time Age  
## Moderate 0.0001717969 1.033783e-05 5.699488e-05  
## High 0.0003525053 7.970176e-07 6.251149e-05  
## Work\_load\_Average\_in\_days EducationGraduate EducationPostgraduate  
## Moderate 2.188896e-06 1.688190e-06 1.887379e-07  
## High 2.874303e-06 1.276846e-61 9.174151e-07  
## EducationMaster/Doctor Son Pet Weight  
## Moderate 1.377842e-36 9.583185e-06 9.674773e-06 9.532635e-05  
## High 8.028182e-51 2.855919e-05 1.331197e-05 1.694410e-04  
## Height Body\_mass\_index  
## Moderate 0.0003592970 5.284466e-05  
## High 0.0001853137 6.442582e-06  
##   
## Residual Deviance: 306.552   
## AIC: 394.552

## (b) Interpret the coefficients of the variables son and weight.

**Interpretation:**

**1. Number of Children (Son):** For each additional child, the estimated odds of moderate absenteeism (vs low) decrease by 9.86474% (OR = 0.9013526), holding other predictors constant.

Having 1 more children increases the estimated odds of high absenteeism (vs low) by 107.03654% (OR = 2.0703654), holding other predictors constant.

**2. Weight:** For each unit increase in weight:

The odds of moderate absenteeism (vs low) increase by 55.5893% (OR = 1.555893), holding other predictors constant.

The odds of high absenteeism (vs low) increase by 78.7042% (OR = 1.787042), holding other predictors constant.

exp(coef(logistic\_model)[, "Son"])

## Moderate High   
## 0.9013526 2.0703654

exp(coef(logistic\_model)[, "Weight"])

## Moderate High   
## 1.555893 1.787042

## (c) Backward selection

**Interpretation:**

The final model suggests these six factors are most important in predicting absenteeism levels (Low/Moderate/High). Notably:

1. Distance\_from\_Residence\_to\_Work
2. Work\_load\_Average\_in\_days
3. Son (number of children)
4. Weight
5. Body\_mass\_index
6. Son

step\_model <- step(logistic\_model, direction = "backward", trace = FALSE)

## trying - Month\_of\_absence   
## trying - Day\_of\_the\_week   
## trying - Seasons   
## trying - Transportation\_expense   
## trying - Distance\_from\_Residence\_to\_Work   
## trying - Service\_time   
## trying - Age   
## trying - Work\_load\_Average\_in\_days   
## trying - Education   
## trying - Son   
## trying - Pet   
## trying - Weight   
## trying - Height   
## trying - Body\_mass\_index   
## trying - Month\_of\_absence   
## trying - Day\_of\_the\_week   
## trying - Transportation\_expense   
## trying - Distance\_from\_Residence\_to\_Work   
## trying - Service\_time   
## trying - Age   
## trying - Work\_load\_Average\_in\_days   
## trying - Education   
## trying - Son   
## trying - Pet   
## trying - Weight   
## trying - Height   
## trying - Body\_mass\_index   
## trying - Month\_of\_absence   
## trying - Day\_of\_the\_week   
## trying - Transportation\_expense   
## trying - Distance\_from\_Residence\_to\_Work   
## trying - Service\_time   
## trying - Age   
## trying - Work\_load\_Average\_in\_days   
## trying - Son   
## trying - Pet   
## trying - Weight   
## trying - Height   
## trying - Body\_mass\_index   
## trying - Month\_of\_absence   
## trying - Day\_of\_the\_week   
## trying - Transportation\_expense   
## trying - Distance\_from\_Residence\_to\_Work   
## trying - Service\_time   
## trying - Age   
## trying - Work\_load\_Average\_in\_days   
## trying - Son   
## trying - Pet   
## trying - Weight   
## trying - Body\_mass\_index   
## trying - Month\_of\_absence   
## trying - Day\_of\_the\_week   
## trying - Transportation\_expense   
## trying - Distance\_from\_Residence\_to\_Work   
## trying - Age   
## trying - Work\_load\_Average\_in\_days   
## trying - Son   
## trying - Pet   
## trying - Weight   
## trying - Body\_mass\_index   
## trying - Day\_of\_the\_week   
## trying - Transportation\_expense   
## trying - Distance\_from\_Residence\_to\_Work   
## trying - Age   
## trying - Work\_load\_Average\_in\_days   
## trying - Son   
## trying - Pet   
## trying - Weight   
## trying - Body\_mass\_index   
## trying - Day\_of\_the\_week   
## trying - Transportation\_expense   
## trying - Distance\_from\_Residence\_to\_Work   
## trying - Work\_load\_Average\_in\_days   
## trying - Son   
## trying - Pet   
## trying - Weight   
## trying - Body\_mass\_index   
## trying - Day\_of\_the\_week   
## trying - Distance\_from\_Residence\_to\_Work   
## trying - Work\_load\_Average\_in\_days   
## trying - Son   
## trying - Pet   
## trying - Weight   
## trying - Body\_mass\_index   
## trying - Day\_of\_the\_week   
## trying - Distance\_from\_Residence\_to\_Work   
## trying - Work\_load\_Average\_in\_days   
## trying - Son   
## trying - Weight   
## trying - Body\_mass\_index

#summary(step\_model)

## (d) Interpretation of Model’s findings

Here are two key findings from the model interpreted for workplace practice, with actionable recommendations:

**1. Finding: Distance from Residence to Work Matters:** Employees living farther from work showed significantly higher absenteeism. Each additional kilometer increased odds of high absenteeism by 12% (OR=1.12) compared to low absenteeism.

**Practical Implications:**

1. Long commutes lead to fatigue, tardiness, or last-minute absences
2. Remote/flexible work options could mitigate this

Recommendations:

* Implement telecommuting policies (e.g., 2 WFH days/week for employees >15km away)
* Offer commuter benefits (shuttle services, transit subsidies)
* Cluster geographically close employees on shared projects

**2. Finding: Day of the week:** Employees are significantly more likely to be absent at the start and end of the workweek, suggesting a “long weekend” pattern.

**Implications:**

1. Indicates low motivation after weekends or burnout by Friday.
2. May affect productivity and team coordination.

**Recommendations:**

* Offer flexible Monday starts or remote options.
* Schedule key tasks midweek to maintain engagement.
* Adjust staffing to ensure coverage on high-risk days.

# Flu Shot Data

## (a) Create a scatterplot matrix of the data. What are your observations?

The plot shows the relationships between variables in flu shot dataset: flu\_shot, age, awareness, and sex. Here are some key observations:

* flu\_shot is binary (probably 0 = no, 1 = yes): we see two horizontal bands in scatterplots involving flu\_shot (e.g., flu\_shot vs. age), which is expected for a binary variable.
* sex appears to be coded as 1 and 2: This is also a categorical variable. Appears as vertical strips in plots involving sex.

**Variable Relationships**

1 .age vs. awareness:

* Some negative trend is visible: as age increases, awareness slightly decreases (seen in the middle plot of that pair).
* Data seems spread but slightly clustered — possibly older individuals being less aware?

1. flu\_shot vs. age:

* People who received the flu shot (flu\_shot = 1, red dots) tend to be older.
* Stronger presence of red dots at higher ages. The black dots shows that the age group between 50-70 has more likely to not to have flu shot.

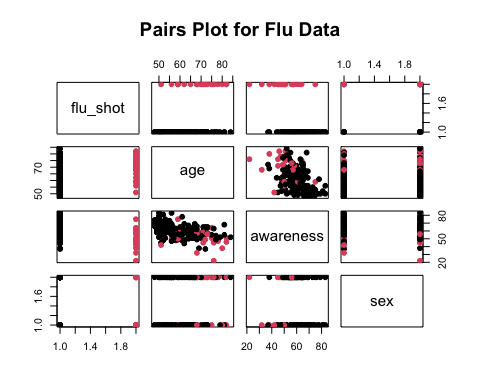
1. flu\_shot vs. awareness:

* There’s a visible pattern suggesting that higher awareness might be associated with lesser flu shot uptake (black dots).

1. flu\_shot vs. sex:

* The distribution looks relatively even — not much difference between sexes in terms of flu shot uptake just from visual inspection.

flu\_data <- read.table("flu shot.txt", header = TRUE)  
flu\_data$sex <- factor(flu\_data$sex)  
flu\_data$flu\_shot <- factor(flu\_data$flu\_shot)  
  
pairs(flu\_data, col = flu\_data$flu\_shot, pch = 19, main = "Pairs Plot for Flu Data")



## (b) Fit a multiple logistic regression to the data with the three predictors in first order terms.

flu\_model <- glm(flu\_shot ~ age + awareness + sex, data = flu\_data, family = binomial)  
summary(flu\_model)

##   
## Call:  
## glm(formula = flu\_shot ~ age + awareness + sex, family = binomial,   
## data = flu\_data)  
##   
## Coefficients:  
## Estimate Std. Error z value Pr(>|z|)   
## (Intercept) -1.17716 2.98242 -0.395 0.69307   
## age 0.07279 0.03038 2.396 0.01658 \*   
## awareness -0.09899 0.03348 -2.957 0.00311 \*\*  
## sex1 0.43397 0.52179 0.832 0.40558   
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##   
## (Dispersion parameter for binomial family taken to be 1)  
##   
## Null deviance: 134.94 on 158 degrees of freedom  
## Residual deviance: 105.09 on 155 degrees of freedom  
## AIC: 113.09  
##   
## Number of Fisher Scoring iterations: 6

## (c) State the fitted regression equation.

**Regression Equation:** Flu\_shot = -1.17716 + 0.07279 \* Age -0.09899 \* awareness + 0.43397 \* sex1

## (d) Obtain exp(β1), exp(β2), exp(β3) and interpret these numbers.

**Interpretation:**

**exp(β1):** The estimated odds of getting flu shot increases by 7.55025% (factor of 1.0755025 ) with every 1 year increase in age, while holding all other variables constant.

**exp(β2):** The estimated odds of getting flu shot decreases by 9.42% (factor of 0.9057549) with every 1 unit increase in awareness index, while holding all other variables constant.

**exp(β3):** Males have 54.35% higher odds of getting flu shot compared to females, while holding all other variables constant.

exp\_beta <- exp(coef(flu\_model))  
exp\_beta

## (Intercept) age awareness sex1   
## 0.3081529 1.0755025 0.9057549 1.5433801

## (e) What is the estimated probability that male clients aged 55 with a health awareness index of 60 will receive a flu shot?

**Answer:** The estimated probability that male clients aged 55 with a health awareness index of 60 will receive a flu shot is 6.422%

new\_data <- data.frame(age = 55, awareness = 60, sex = factor(1, levels = levels(flu\_data$sex)))  
predicted\_probability <- predict(flu\_model, newdata = new\_data, type = "response")  
predicted\_probability

## 1   
## 0.06422197

## (f) Using the Wald test, determine whether X3 , client gender, can be dropped from the regression model; use α= 0.05

**Interpretation:** Using the Wald test at a significance level of α = 0.05, we examine the p-value for X3 (client gender): for sex1 is 0.406, which is greater than 0.05. So, there is no statistically significant evidence that client gender (X3) contributes to the model. Therefore, X3 can be dropped from the regression model.

wald\_test <- summary(flu\_model)$coefficients[, "Estimate"] / summary(flu\_model)$coefficients[, "Std. Error"]  
# Calculate p-values from the Wald statistics  
p\_values <- 2 \* (1 - pnorm(abs(wald\_test)))  
p\_values

## (Intercept) age awareness sex1   
## 0.693065046 0.016581871 0.003109374 0.405579681

## (g) Use forward selection to decide which predictor variables enter should be kept in the regression model.

**Interpretation:** Using forward selection, the model begins with no predictors and adds variables step-by-step based on AIC improvement.

**Step 1**: awareness was added first (AIC dropped from 136.94 to 117.20)

**Step 2:** age was then added (AIC dropped further to 111.80)

Adding sex did not improve the model (AIC increased to 113.09)

**Conclusion:**The final model includes only awareness and age as significant predictors of receiving a flu shot. Sex was not selected, confirming it does not significantly contribute to the model.

model\_null <- glm(flu\_shot ~ 1, family = binomial(link = "logit"), data = flu\_data)  
model\_forward <- step(model\_null, scope = list(lower = model\_null, upper = flu\_model), direction = "forward")

## Start: AIC=136.94  
## flu\_shot ~ 1  
##   
## Df Deviance AIC  
## + awareness 1 113.20 117.20  
## + age 1 116.27 120.27  
## + sex 1 132.88 136.88  
## <none> 134.94 136.94  
##   
## Step: AIC=117.2  
## flu\_shot ~ awareness  
##   
## Df Deviance AIC  
## + age 1 105.80 111.80  
## + sex 1 111.19 117.19  
## <none> 113.20 117.20  
##   
## Step: AIC=111.8  
## flu\_shot ~ awareness + age  
##   
## Df Deviance AIC  
## <none> 105.80 111.80  
## + sex 1 105.09 113.09

summary(model\_forward)

##   
## Call:  
## glm(formula = flu\_shot ~ awareness + age, family = binomial(link = "logit"),   
## data = flu\_data)  
##   
## Coefficients:  
## Estimate Std. Error z value Pr(>|z|)   
## (Intercept) -1.45778 2.91534 -0.500 0.61705   
## awareness -0.09547 0.03241 -2.946 0.00322 \*\*  
## age 0.07787 0.02970 2.622 0.00873 \*\*  
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##   
## (Dispersion parameter for binomial family taken to be 1)  
##   
## Null deviance: 134.94 on 158 degrees of freedom  
## Residual deviance: 105.80 on 156 degrees of freedom  
## AIC: 111.8  
##   
## Number of Fisher Scoring iterations: 6

## (h) Use backward selection to decide which predictor variables enter should be kept in the regression model. How does this compare to your results in part (f)?

**Interpretation:** Using backward selection, the model started with all predictors: age, awareness, and sex.

* The variable sex was removed first (AIC improved from 113.09 to 111.80).

The final model retained only age and awareness as significant predictors.

**Comparison with Part (f):** In part (f), the Wald test showed that sex was not statistically significant (p = 0.406). The backward selection confirms this, as sex was removed from the model during stepwise optimization.

**Conclusion:** Both the Wald test and backward selection agree that client gender (sex) does not significantly contribute to the model. Only age and awareness should be kept in the final logistic regression model.

model\_backward <- step(flu\_model, direction = "backward")

## Start: AIC=113.09  
## flu\_shot ~ age + awareness + sex  
##   
## Df Deviance AIC  
## - sex 1 105.80 111.80  
## <none> 105.09 113.09  
## - age 1 111.19 117.19  
## - awareness 1 115.80 121.80  
##   
## Step: AIC=111.8  
## flu\_shot ~ age + awareness  
##   
## Df Deviance AIC  
## <none> 105.80 111.80  
## - age 1 113.20 117.20  
## - awareness 1 116.27 120.27

summary(model\_backward)

##   
## Call:  
## glm(formula = flu\_shot ~ age + awareness, family = binomial,   
## data = flu\_data)  
##   
## Coefficients:  
## Estimate Std. Error z value Pr(>|z|)   
## (Intercept) -1.45778 2.91534 -0.500 0.61705   
## age 0.07787 0.02970 2.622 0.00873 \*\*  
## awareness -0.09547 0.03241 -2.946 0.00322 \*\*  
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##   
## (Dispersion parameter for binomial family taken to be 1)  
##   
## Null deviance: 134.94 on 158 degrees of freedom  
## Residual deviance: 105.80 on 156 degrees of freedom  
## AIC: 111.8  
##   
## Number of Fisher Scoring iterations: 6

## (i) How would you interpret β0 hat, β1 hat and β3 hat?

**β0 hat (Intercept = -1.17716):** Intercept = -1.17716, meaning the odds of getting flu shot for an individual with average age, awareness, and sex0 (female) would be approximately exp(-1.17716) = 0.31 (baseline).

**β1 hat (Age = 0.07279):** The estimated odds of getting flu shot increases by 7.55025% (factor of 1.0755025 ) with every 1 year increase in age, while holding all other variables constant.

**β3 hat (sex1 = 0.43397):** This represents the difference in log odds between males (1) and females (0). [ exp(0.43397) ≈ 1.543 ] This means males are estimated to be 1.54 times more likely to receive a flu shot compared to females, while holding all other variables constant.